Effect of Ballistic Electrons on the Optical Response of Hyperbolic Metamaterials

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Abstract

This paper presents a theoretical and experimental study of the effect of ballistic electrons on the optical response of MIM (Metal-Insulator-Metal) like hyperbolic metamaterial structures. The simulated model using standard parameters and the experimental optical transmission show a 20% peak difference due to the presence of ballistic transport in the metal. A semi-analytic approximation based on the Drude’s model is used for accurately predicting the optical response of the hyperbolic substrate and plasmon damping in the fabricated metasurfaces.

1. Introduction

Metamaterials, especially those designed for operating in the visible spectrum, enable deeper control of light. By engineering its primitive components, also called meta-atoms, the light pathway can be precisely controlled. Better and uncommon optical components [1, 2, 3] can be realized choosing the distribution and the correct meta-atoms.

In special, hyperbolic metamaterials have been attracting attention due to the possibility of light confinement at the nanoscale. This class of metamaterials has its isofrequency surface unbounded and defined by a hyperboloid. While the wave propagation vector (k) is not restricted to a finite number, the wavelength can achieve infinitely small values [4, 5]. The only limit for the wavelength compression is defined by the non-ideal physical properties of its constituent material [6] and by the significant losses at high-frequency operation [7, 8]. This exotic property permits electric field confinement causing a spontaneous emission enhancement leading to a large Purcell factor [9, 10, 11]. Emerging applications on lasing [12], LED’s [13, 14] sensing [15, 16], imaging [17, 18] and absorbers [19] have been recently reported showing the interest for continued efforts in this area.

However, in the design of these devices, thin layers of metals with precise thickness are often used. As the metal thickness decreases, the effect of ballistic electrons is neglected as the models are usually fitted for a single thickness. Experimentally, this is seen by the increase of optical attenuation in the transmitted light.

Here, we present a theoretical and experimental study of the effect of ballistic electrons on the optical response of a MIM (Metal-Insulator-Metal) hyperbolic metamaterial structure consisting of silver and silicon dioxide thin films. A semi-analytical model was constructed based on the experimental data and the Drude’s model with ballistic transport considerations. Finally, the effect of increased electron damping behavior was analyzed relative to the plasmonic behavior of the structure.

2. Optical response of silver thin films

Drude’s model is the classical way of explaining the optical response of metals. However, when the mean free path of electrons in the material is comparable to its thickness, an extended description must be considered taking into account the effect of ballistic electrons on the material’s complex permittivity.

2.1. Drude Model

The Drude’s model considers that the electrons aren’t bounded and move freely in a given metal. Hence, electrons excited by an exterior electromagnetic field move accordingly to the field, only limited by the viscosity of the electrons in the metallic lattice. Mathematically, the movement is similar to a harmonic oscillator, Equation 1, where m: represents the electron mass; Γ: the damping factor; e: the electron charge; r(t): the electron movement; and E(t): the electromagnetic excitation.

\[ m \frac{\partial^2 r(t)}{\partial t^2} + m \Gamma \frac{\partial r(t)}{\partial t} = -e \vec{E}_0 e^{-i \omega t} \]  

The electronic movement induced by the exterior field defines the optical response of the material. The complex permittivity is given by Equation 2 as a consequence of Equation 1, where \( \omega_p \): plasma frequency; \( \Gamma \): the damping factor; and \( \varepsilon_\infty \): the offset permittivity due to bounded electrons in the material [20].

\[ \varepsilon(\omega) = \varepsilon_\infty - \frac{\omega_p^2}{\omega^2 + \Gamma^2} + i \frac{\omega_p \Gamma}{\omega(\omega^2 + \Gamma^2)} \]  

2.2. Optical Response of Silver Thin Films

Physically, the damping has a direct relation to the mean free path of the electron in the metal. The smaller the electron difficult in moving, the longer the mean free path. However, especially for silver which has a mean-free path...
of 53.3 nm [21], films of the order of tenths of nanometers impose a new boundary on the electron’s movement, therefore increasing the damping effect. These electrons have now a ballistic motion due to the interface limitation as the thickness of the film is smaller than the mean-free path.

Equation 3 shows how the interface thickness (R) relates to the damping factor increase (Γ∗), where \( v_F \) : Fermi velocity and \( a \) : prefactor dependent on the geometry [20].

\[
Γ^* = Γ + a \frac{v_F}{R} \tag{3}
\]

Figure 1: Drude’s model of the silver Permittivity as function of the wavelength for different thicknesses as shown in Figure 1. The numerical values of silver constants are taken from the data available for silver in Cai and Shalaev [20] where \( Γ = 0.032 \times 10^{15} \text{ s}^{-1} \) , \( ω_p = 14.0 \times 10^{15} \text{ rad/s} \) and \( v_F = 1.4 \times 10^6 \text{ m/s} \) and \( a = 1 \) due to geometric symmetry of a continuous film.

Using equations 2 and 3, we construct the permittivity as function of the wavelength for different thicknesses. As shown in Figure 1. The real part of the permittivity \( ε(ω) \) is defined as

\[
α_L(ω) = \frac{Real(ε_{Drude}(ω))_{L}}{Real(ε_{Drude}(ω))_{30nm}} \tag{4}
\]

\[
β_L(ω) = \frac{Im(ε_{Drude}(ω))_{L}}{Im(ε_{Drude}(ω))_{30nm}} \tag{5}
\]

To calculate the permittivity of a film with thickness L \( ε(ω, L) \) it is necessary to rescale the real and imaginary part of the permittivity of a 30nm thick thilm experimental obtained using the analytical coefficients \( α_L(ω) \) and \( β_L(ω) \) as presented Equation (6).

\[
ε^*(ω, L) = α_L(ω). Real(ε(ω))_{30nm} + i.β_L(ω).Im(ε(ω))_{30nm} \tag{6}
\]

2.3. Addition of ballistic effects in Experimental Data

Although the modeling of the ballistic effect in thin films is expressed analytically in the Drude’s model, the real optical behavior of materials takes into account external orbital interactions and atom bounded states. Nevertheless, the available experimental fit for materials usually is done for a single thickness and it does not considers the ballistic effect of electrons. For example, Palik’s data for silver consider films 30nm [22] thick. Hence, for verifying the validity of the standard silver model, the transmission of a 30 nm thermally evaporated silver film is compared to Palik’s, CRC’s and Jonshon and Christy’s models in Figure 2.

However, the experimental and simulated models are only valid for this thickness due to ballistic electrons effects in thinner thickness. Therefore, we use a semi-analytical method for improving the simulation results taking into account ballistic electrons effects. Our approach is capable of calculating the permittivity of thin silver films with any thickness (L) by scaling the experimental data of single thickness using two coefficients \( α_L(ω) \) and \( β_L(ω) \) analytically extracted from the Drude Model. The coefficients \( α_L(ω) \) and \( β_L(ω) \) are defined as the ratio between the real and imaginary part, respectively, of the permittivity of a film with thickness L and 30nm obtained via the Drude model as follows,

Figure 2: Experimental and simulated transmission of a 30 nm silver film for CRC’s, Palik’s and Jonhson and Christy’s models.

2.4. Optical Response of Hyperbolic Substrate

The hyperbolic substrate considered in this paper is a multilayered MIM (Metal-Insulator-Metal) structure (9 in total) over a glass substrate.
The top layer is a 7.5 nm silver layer with the remaining layers consisting of a periodic stack of 15 nm silver (Ag) and 60 nm silicon oxide (SiO$_2$) [15]. Figure 4(a) is the three dimensional model of such structure.

The fabrication of this film is done by alternating cycles of thermal evaporation for silver layers, and e-beam evaporation for the silicon dioxide layers. The thickness was controlled via standard oscillator frequency shift method embedded in both evaporators, and the total thickness was controlled by a Dektak XT Profilometer.

Figure 4(b) shows the film optical response for experimental and simulated substrates. The experimental optical response is obtained using a UV-Vis spectrometer. The optical transmission of the hyperbolic substrate is numerically obtained with the software FDTD Lumerical© considering initially the standard CRC model, and then, the CRC model with the proposed correction described in the previous section. Figure 4(c) shows the simulated electric fields for different wavelengths.

2.5. Optical Response of Hyperbolic Metasurfaces

In this work, two metasurfaces were studied, a linear array of slits with 250 nm period and 50 nm width and a concentric array of circular rings with 50 nm width separated by 350 nm. They were fabricated over a 20μm × 20μm surface. Both structures were fabricated using a focused ion beam for milling the pattern on the multilayer structure.

Figures 4(a) and 5(a) show the 3D modeling of the structures, and figures 4(b) and 5(b) the SEM images of the fabricated structure.

The simulation of both structures was carried out using the previous model with ballistic effects using symme-
Figure 4: (a) 3D model of a linear array of slits on a metasurface. (b) SEM image of a linear array of slits with 250 nm period and 50 nm width. (c) Simulated normalized transmission spectrum of the metasurface for TE and TM modes and field maps. (d) and (e) are the far-field optical images of the transmitted through the film and the metasurface region as indicated in (b) with the incoming light polarized parallel (TE) to the slits and perpendicular (TM).

3. Discussions

Figure 4(b) shows the simulated results obtained with both models (standard and corrected) and experimental results with almost the same behavior in the blue spectral range. However, as can be seen in Figure 4(b), the transmission calculated with the proposed correction presents a much better agreement with the experimental curve than the CRC model without the correction. The CRC model does not take the ballistic electron into account, which outcomes in a smaller permittivity imaginary part. Hence, in a higher transmission as observed in Figure 4(b), the experimental data shows a peak transmission of about 20% lower than the one simulated using bulk silver parameters. The mismatch observed near the pick happens due to an interpolation inaccuracy in the simulation results.

This same effect must be considered in the treatment of the light transmitted through the metasurfaces region. As the electron mobility decreases, the plasmon quality may also decrease due to the greater material resistance. Using the semi-analytic approximation, a more reliable simulation of the proposed metastructures in the Figures 4(a) and 5(a) can be obtained.

The optical transmission of the linear array of slits for TE polarization, 4(c), shows a blue spectra similar to the
one observed in Figure 4(d). The TM polarized wave, in turn, shows a blue-green spectra similar to the one observed in Figure 4(e). Similarly, the same is observed for the array of concentric rings. The simulation predicts a weak red signal with emission in two principal lobes which are verified in the optical image using a red filter. The blue light transmission seen in the spectrum is due to the transmission mainly from the substrate without interacting with the structure. Also, Figure 5(c) shows the damping in the plasmonic response while considering the ballistic transport.

4. Conclusions

This paper has investigated the effect of ballistic electrons in silver thin films and how they impact the attenuation factor of simulated structures when compared to experimental results of hyperbolic metasurfaces. The ballistic transport also affects the plasmon quality in the structure due to increased resistance in its transport. A proposed semi-analytical approximation based on ballistic electrons effects in the Drude’s model is used to accurately predict the optical response of hyperbolic metasurfaces.

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References


